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1 Quantitative T1 MRI

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7 Summary

8 This NeuroLibre Reproducible preprint is an interactive tutorial on quantitative T1 mapping
9 MRI. It is an interactive version of two subsections of the chapter “Quantitative T1 and T1r
10 Mapping” in the book Quantitative Magnetic Resonance Imaging ([Boudreau et al., 2020](#)).



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25 About

26 This Jupyter Book is a series of interactive tutorials about quantitative T1 mapping, powered
27 by [qMRLab](#) ([Karakuzu et al., 2020](#)).

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31 Inversion Recovery T1 Mapping

32 Widely considered the gold standard for T1 mapping, the inversion recovery technique estimates
 33 T1 values by fitting the signal recovery curve acquired at different delays after an inversion
 34 pulse (180°). In a typical inversion recovery experiment (Figure 1), the magnetization at
 35 thermal equilibrium is inverted using a 180° RF pulse. After the longitudinal magnetization
 36 recovers through spin-lattice relaxation for predetermined delay (“inversion time”, TI), a 90°
 37 excitation pulse is applied, followed by a readout imaging sequence (typically a spin-echo or
 38 gradient-echo readout) to create a snapshot of the longitudinal magnetization state at that TI.

39 Inversion recovery was first developed for NMR in the 1940s (Drain, 1949; Hahn, 1949), and
 40 the first T1 map was acquired using a saturation-recovery technique (90° as a preparation pulse
 41 instead of 180°) by (Pykett & Mansfield, 1978). Some distinct advantages of inversion recovery
 42 are its large dynamic range of signal change and an insensitivity to pulse sequence parameter
 43 imperfections (Stikov et al., 2015). Despite its proven robustness at measuring T1, inversion
 44 recovery is scarcely used in practice, because conventional implementations require repetition
 45 times (TRs) on the order of 2 to 5 T1 (Steen et al., 1994), making it challenging to acquire
 46 whole-organ T1 maps in a clinically feasible time. Nonetheless, it is continuously used as a
 47 reference measurement during the development of new techniques, or when comparing different
 48 T1 mapping techniques, and several variations of the inversion recovery technique have been
 49 developed, making it practical for some applications (Messroghli et al., 2004; Piechnik et al.,
 50 2010).

51 **Figure 1. Pulse sequence of an inversion recovery experiment.**

52 Signal Modelling

53 The steady-state longitudinal magnetization of an inversion recovery experiment can be derived
 54 from the Bloch equations for the pulse sequence {θ180 – TI – θ90 – (TR-TI)}, and is given by:

$$M_z(TI) = M_0 \frac{1 - \cos(\theta_{180})e^{-\frac{TR}{T_1}} - [1 - \cos(\theta_{180})]e^{-\frac{TI}{T_1}}}{1 - \cos(\theta_{180})\cos(\theta_{90})e^{-\frac{TR}{T_1}}} \quad (1)$$

55 where M_z is the longitudinal magnetization prior to the θ90 pulse. If the in-phase real signal
 56 is desired, it can be calculated by multiplying Eq. 1 by $k\sin(\theta_{90})e^{-TE/T_2}$, where k is a
 57 constant. This general equation can be simplified by grouping together the constants for each
 58 measurements regardless of their values (i.e. at each TI, same TE and θ90 are used) and
 59 assuming an ideal inversion pulse:

$$M_z(TI) = C(1 - 2e^{-\frac{TI}{T_1}} + e^{-\frac{TR}{T_1}}) \quad (2)$$

60 where the first three terms and the denominator of Eq. 1 have been grouped together into the
 61 constant C . If the experiment is designed such that TR is long enough to allow for full relaxation
 62 of the magnetization (TR > 5T1), we can do an additional approximation by dropping the
 63 last term in Eq. 2:

$$M_z(TI) = C(1 - 2e^{-\frac{TI}{T_1}}) \quad (3)$$

64 The simplicity of the signal model described by Eq. 3, both in its equation and experimental
 65 implementation, has made it the most widely used equation to describe the signal evolution
 66 in an inversion recovery T1 mapping experiment. The magnetization curves are plotted in
 67 Figure 2 for approximate T1 values of three different tissues in the brain. Note that in many
 68 practical implementations, magnitude-only images are acquired, so the signal measured would
 69 be proportional to the absolute value of Eq. 3.

70 **Figure 2.** Inversion recovery curves (Eq. 2) for three different T1 values, approximating the
71 main types of tissue in the brain.

72 Practically, Eq. 1 is the better choice for simulating the signal of an inversion recovery
73 experiment, as the TRs are often chosen to be greater than 5T1 of the tissue-of-interest, which
74 rarely coincides with the longest T1 present (e.g. TR may be sufficiently long for white matter,
75 but not for CSF which could also be present in the volume). Equation 3 also assumes ideal
76 inversion pulses, which is rarely the case due to slice profile effects. **Figure 3** displays the
77 inversion recovery signal magnitude (complete relaxation normalized to 1) of an experiment
78 with TR = 5 s and T1 values ranging between 250 ms to 5 s, calculated using both equations.

79 **Figure 3.** Signal recovery curves simulated using Eq. 3 (solid) and Eq. 1 (dotted) with a TR
80 = 5 s for T1 values ranging between 0.25 to 5 s.

81 Data Fitting

82 Several factors impact the choice of the inversion recovery fitting algorithm. If only magnitude
83 images are available, then a polarity-inversion is often implemented to restore the non-
84 exponential magnitude curves (**Figure 3**) into the exponential form (**Figure 2**). This process is
85 sensitive to noise due to the Rician noise creating a non-zero level at the signal null. If phase
86 data is also available, then a phase term must be added to the fitting equation (**Barral et al.,**
87 **2010**). Equation 3 must only be used to fit data for the long TR regime (TR > 5T1), which
88 in practice is rarely satisfied for all tissues in subjects.

89 Early implementations of inversion recovery fitting algorithms were designed around the
90 computational power available at the time. These included the “null method” (**Pykett et**
91 **al., 1983**), assuming that each T1 value has unique zero-crossings (see **Figure 2**), and linear
92 fitting of a rearranged version of Eq. 3 on a semi-log plot (**Fukushima, 1981**). Nowadays, a
93 non-linear least-squares fitting algorithm (e.g. Levenberg-Marquardt) is more appropriate, and
94 can be applied to either approximate or general forms of the signal model (Eq. 3 or Eq. 1).
95 More recent work (**Barral et al., 2010**) demonstrated that T1 maps can also be fitted much
96 faster (up to 75 times compared to Levenberg-Marquardt) to fit Eq. 1 – without a precision
97 penalty – by using a reduced-dimension non-linear least squares (RD-NLS) algorithm. It was
98 demonstrated that the following simplified 5-parameter equation can be sufficient for accurate
99 T1 mapping:

$$S(TI) = a + be^{-\frac{TI}{T_1}} \quad (4)$$

100 where a and b are complex values. If magnitude-only data is available, a 3-parameter model
101 can be sufficient by taking the absolute value of Eq. 4. While the RD-NLS algorithms are too
102 complex to be presented here (the reader is referred to the paper, (**Barral et al. 2010**)), the
103 code for these algorithms **was released open-source** along with the original publication, and is
104 also available as a **qMRLab** T1 mapping model. One important thing to note about Eq. 4 is
105 that it is general – no assumption is made about TR – and is thus as robust as Eq. 1 as long
106 as all pulse sequence parameters other than T1 are kept constant between each measurement.

107 **Figure 4** compares simulated data (Eq. 1) using a range of TRs (1.5T1 to 5T1) fitted using
108 either RD-NLS & Eq. 4 or a Levenberg-Marquardt fit of Eq. 2.

109 **Figure 4.** Fitting comparison of simulated data (blue markers) with T1 = 1 s and TR =
110 1.5 to 5 s, using fitted using RD-NLS & Eq. 4 (green) and Levenberg-Marquardt & Eq. 2
111 (orange, long TR approximation).

112 **Figure 5** displays an example brain dataset from an inversion recovery experiment, along with
113 the T1 map fitted using the RD-NLS technique.

114 **Figure 5.** Example inversion recovery dataset of a healthy adult brain (left). Inversion times
115 used to acquire this magnitude image dataset were 30 ms, 530 ms, 1030 ms, and 1530 ms,
116 and the TR used was 1550 ms. The T1 map (right) was fitted using a RD-NLS algorithm.

117 Benefits and Pitfalls

118 The conventional inversion recovery experiment is considered the gold standard T1 mapping
119 technique for several reasons:

- 120 ▪ A typical protocol has a long TR value and a sufficient number of inversion times for
121 stable fitting (typically 5 or more) covering the range $[0, TR]$.
- 122 ▪ It offers a wide dynamic range of signals (up to $[-kM_0, kM_0]$), allowing a number
123 of inversion times where high SNR is available to sample the signal recovery curve
124 ([Fukushima, 1981](#)).
- 125 ▪ T1 maps produced by inversion recovery are largely insensitive to inaccuracies in excitation
126 flip angles and imperfect spoiling ([Stikov et al., 2015](#)), as all parameters except T1 are
127 constant for each measurement and only a single acquisition is performed (at T1) during
128 each TR.

129 One important protocol design consideration is to avoid acquiring at inversion times where
130 the signal for T1 values of the tissue-of-interest is nulled, as the magnitude images at this
131 TI time will be dominated by Rician noise which can negatively impact the fit under low
132 SNR circumstances ([Figure 6](#)). Inversion recovery can also often be acquired using commonly
133 available standard pulse sequences available on most MRI scanners by setting up a customized
134 acquisition protocol, and does not require any additional calibration measurements. For an
135 example, please visit the interactive preprint of the ISMRM Reproducible Research Group 2020
136 Challenge on inversion recovery T1 mapping ([Boudreau et al., 2023](#)).

137 **Figure 6.** Monte Carlo simulations (mean and standard deviation (STD), blue markers) and
138 fitted T1 values (mean and STD, red and green respectively) generated for a T1 value of
139 900 ms and 5 T1 values linearly spaced across the TR (ranging from 1 to 5 s). A bump in
140 T1 STD occurs near $TR = 3000$ ms, which coincides with the TR where the second T1 is
141 located near a null point for this T1 value.

142 Despite a widely acknowledged robustness for measuring accurate T1 maps, inversion recovery
143 is not often used in studies. An important drawback of this technique is the need for long TR
144 values, generally on the order of a few T1 for general models (e.g. Eqs. 1 and 4), and up to
145 5T1 for long TR approximated models (Eq. 3). It takes about to 10-25 minutes to acquire a
146 single-slice T1 map using the inversion recovery technique, as only one TI is acquired per TR
147 (2-5 s) and conventional cartesian gradient readout imaging acquires one phase encode line
148 per excitation (for a total of ~ 100 -200 phase encode lines). The long acquisition time makes it
149 challenging to acquire whole-organ T1 maps in clinically feasible protocol times. Nonetheless,
150 it is useful as a reference measurement for comparisons against other T1 mapping methods, or
151 to acquire a single-slice T1 map of a tissue to get T1 estimates for optimization of other pulse
152 sequences.

153 Other Saturation-Recovery T1 Mapping techniques

154 Several variations of the inversion recovery pulse sequence were developed to overcome
155 challenges like those specified above. Amongst them, the Look-Locker technique ([Look &
156 Locker, 1970](#)) stands out as one of the most widely used in practice. Instead of a single 90°
157 acquisition per TR, a periodic train of small excitation pulses θ are applied after the inversion
158 pulse, $\{\theta 180 - -\theta - -\theta - \dots\}$, where $\theta = TR/n$ and n is the number of sampling acquisitions.
159 This pulse sequence samples the inversion time relaxation curve much more efficiently than
160 conventional inversion recovery, but at a cost of lower SNR. However, because the magnetization
161 state of each TI measurement depends on the previous series of θ excitation, it has higher
162 sensitivity to B1-inhomogeneities and imperfect spoiling compared to inversion recovery ([Gai et
163 al., 2013](#); [Stikov et al., 2015](#)). Nonetheless, Look-Locker is widely used for rapid T1 mapping
164 applications, and variants like MOLLI (Modified Look-Locker Inversion recovery) and ShMOLLI
165 (Shortened MOLLI) are widely used for cardiac T1 mapping ([Messroghli et al., 2004](#); [Piechnik
166 et al., 2010](#)).

167 Another inversion recovery variant that's worth mentioning is saturation recovery, in which the
 168 inversion pulse is replaced with a saturation pulse: $\{\theta 90 - T1 - \theta 90\}$. This technique was used
 169 to acquire the very first T1 map (Pykett & Mansfield, 1978). Unlike inversion recovery, this
 170 pulse sequence does not need a long TR to recover to its initial condition; every $\theta 90$ pulse
 171 resets the longitudinal magnetization to the same initial state. However, to properly sample the
 172 recovery curve, TIs still need to reach the order of $\sim T1$, the dynamic range of signal potential
 173 is cut in half ($[0, M0]$), and the short TIs (which have the fastest acquisition times) have the
 174 lowest SNRs.

175 Variable Flip Angle T1 Mapping

176 Variable flip angle (VFA) T1 mapping (Christensen et al., 1974; Fram et al., 1987; Gupta,
 177 1977), also known as Driven Equilibrium Single Pulse Observation of T1 (DESPOT1) (Deoni
 178 et al., 2003; Homer & Beevers, 1985), is a rapid quantitative T1 measurement technique
 179 that is widely used to acquire 3D T1 maps (e.g. whole-brain) in a clinically feasible time.
 180 VFA estimates T1 values by acquiring multiple spoiled gradient echo acquisitions, each with
 181 different excitation flip angles (θ_n for $n = 1, 2, \dots, N$ and $\theta_i \neq \theta_j$). The steady-state signal of
 182 this pulse sequence (Figure 1) uses very short TRs (on the order of magnitude of 10 ms) and
 183 is very sensitive to T1 for a wide range of flip angles.

184 VFA is a technique that originates from the NMR field, and was adopted because of its time
 185 efficiency and the ability to acquire accurate T1 values simultaneously for a wide range of
 186 values (Christensen et al., 1974; Gupta, 1977). For imaging applications, VFA also benefits
 187 from an increase in SNR because it can be acquired using a 3D acquisition instead of multislice,
 188 which also helps to reduce slice profile effects. One important drawback of VFA for T1 mapping
 189 is that the signal is very sensitive to inaccuracies in the flip angle value, thus impacting the T1
 190 estimates. In practice, the nominal flip angle (i.e. the value set at the scanner) is different
 191 than the actual flip angle experienced by the spins (e.g. at 3.0 T, variations of up to $\pm 30\%$),
 192 an issue that increases with field strength. VFA typically requires the acquisition of another
 193 quantitative map, the transmit RF amplitude ($B1+$, or $B1$ for short), to calibrate the nominal
 194 flip angle to its actual value because of $B1$ inhomogeneities that occur in most loaded MRI
 195 coils (Sled & Pike, 1998). The need to acquire an additional $B1$ map reduces the time savings
 196 offered by VFA over saturation-recovery techniques, and inaccuracies/imprecisions of the $B1$
 197 map are also propagated into the VFA T1 map (Boudreau et al., 2017; Lee et al., 2017).

198 **Figure 1.** Simplified pulse sequence diagram of a variable flip angle (VFA) pulse sequence
 199 with a gradient echo readout. TR: repetition time, θ_n : excitation flip angle for the n th
 200 measurement, IMG: image acquisition (k-space readout), SPOIL: spoiler gradient.

201 Signal Modelling

202 The steady-state longitudinal magnetization of an ideal variable flip angle experiment can
 203 be analytically solved from the Bloch equations for the spoiled gradient echo pulse sequence
 204 $\{\theta_n - TR\}$:

$$M_z(\theta_n) = M_0 \frac{1 - e^{-\frac{TR}{T_1}}}{1 - \cos(\theta_n) e^{-\frac{TR}{T_1}}} \sin(\theta_n) \quad (1)$$

205 where M_z is the longitudinal magnetization, M_0 is the magnetization at thermal equilibrium,
 206 TR is the pulse sequence repetition time (Figure 1), and θ_n is the excitation flip angle. The
 207 M_z curves of different T1 values for a range of θ_n and TR values are shown in Figure 2.

208 **Figure 2.** Variable flip angle technique signal curves (Eq. 1) for three different T1 values,
 209 approximating the main types of tissue in the brain at 3T.

210 From **Figure 2**, it is clearly seen that the flip angle at which the steady-state signal is maximized
 211 is dependent on the T1 and TR values. This flip angle is a well known quantity, called the
 212 Ernst angle (**Ernst & Anderson, 1966**), which can be solved analytically from Equation 1 using
 213 properties of calculus:

$$\theta_{Ernst} = \arccos\left(e^{-\frac{TR}{T_1}}\right) \quad (2)$$

214 The closed-form solution (Equation 1) makes several assumptions which in practice may not
 215 always hold true if care is not taken. Mainly, it is assumed that the longitudinal magnetization
 216 has reached a steady state after a large number of TRs, and that the transverse magnetization
 217 is perfectly spoiled at the end of each TR. Bloch simulations – a numerical approach at solving
 218 the Bloch *equations* for a set of spins at each time point – provide a more realistic estimate of
 219 the signal if the number of repetition times is small (i.e. a steady-state is not achieved). As
 220 can be seen from **Figure 3**, the number of repetitions required to reach a steady state not only
 221 depends on T1, but also on the flip angle; flip angles near the Ernst angle need more TRs
 222 to reach a steady state. Preparation pulses or an outward-in k-space acquisition pattern are
 223 typically sufficient to reach a steady state by the time that the center of k-space is acquired,
 224 which is where most of the image contrast resides.

225 **Figure 3.** Signal curves simulated using Bloch simulations (orange) for a number of repetitions
 226 ranging from 1 to 150, plotted against the ideal case (Equation 1 – blue). Simulation
 227 details: TR = 25 ms, T1 = 900 ms, 100 spins. Ideal spoiling was used for this set of Bloch
 228 simulations (transverse magnetization was set to 0 at the end of each TR).

229 Sufficient spoiling is likely the most challenging parameter to control for in a VFA experiment.
 230 A combination of both gradient spoiling and RF phase spoiling (**Bernstein et al., 2004; Zur et
 231 al., 1991**) are typically recommended (**Figure 4**). It has also been shown that the use of very
 232 strong gradients, introduces diffusion effects (not considered in **Figure 4**), further improving
 233 the spoiling efficacy in the VFA pulse sequence (**Yarnykh, 2010**).

234 **Figure 4.** Signal curves estimated using Bloch simulations for three categories of signal
 235 spoiling: (1) ideal spoiling (blue), gradient & RF Spoiling (orange), and no spoiling (green).
 236 Simulations details: TR = 25 ms, T1 = 900 ms, Te = 100 ms, TE = 5 ms, 100 spins. For
 237 the ideal spoiling case, the transverse magnetization is set to zero at the end of each TR.
 238 For the gradient & RF spoiling case, each spin is rotated by different increments of phase (2
 239 / # of spins) to simulate complete decoherence from gradient spoiling, and the RF phase of
 240 the excitation pulse is $\phi_n = \phi_{n-1} + n\phi_0 = \frac{1}{2} \phi_0(n^2 + n + 2)$ (**Bernstein et al., 2004**)
 241 with $\phi_0 = 117^\circ$ (**Zur et al., 1991**) after each TR.

242 Data Fitting

243 At first glance, one could be tempted to fit VFA data using a non-linear least squares fitting
 244 algorithm such as Levenberg-Marquardt with Eq. 1, which typically only has two free fitting
 245 variables (T1 and M0). Although this is a valid way of estimating T1 from VFA data, it is
 246 rarely done in practice because a simple refactoring of Equation 1 allows T1 values to be
 247 estimated with a linear least square fitting algorithm, which substantially reduces the processing
 248 time. Without any approximations, Equation 1 can be rearranged into the form $y = mx+b$
 249 (**Gupta, 1977**):

$$\frac{S_n}{\sin(\theta_n)} = e^{-\frac{TR}{T_1}} \frac{S_n}{\tan(\theta_n)} + C(1 - e^{-\frac{TR}{T_1}}) \quad (3)$$

250 As the third term does not change between measurements (it is constant for each θ_n), it can
 251 be grouped into the constant for a simpler representation:

$$\frac{S_n}{\sin(\theta_n)} = e^{-\frac{TR}{T_1}} \frac{S_n}{\tan(\theta_n)} + C \quad (4)$$

252 With this rearranged form of Equation 1, T1 can be simply estimated from the slope of a linear
253 regression calculated from $S_n/\sin(\theta_n)$ and $S_n/\tan(\theta_n)$ values:

$$T_{_1} = -\frac{TR}{\ln(\text{slope})} \quad (5)$$

254 If data were acquired using only two flip angles – a very common VFA acquisition protocol –
255 then the slope can be calculated using the elementary slope equation. **Figure 5** displays both
256 Equation 1 and 4 plotted for a noisy dataset.

257 **Figure 5.** Mean and standard deviation of the VFA signal plotted using the nonlinear form
258 (Equation 1 – blue) and linear form (Equation 4 – red). Monte Carlo simulation details:
259 SNR = 25, N = 1000. VFA simulation details: TR = 25 ms, T1 = 900 ms.

260 There are two important imaging protocol design considerations that should be taken into
261 account when planning to use VFA: (1) how many and which flip angles to use to acquire
262 VFA data, and (2) correcting inaccurate flip angles due to transmit RF field inhomogeneity.
263 Most VFA experiments use the minimum number of required flip angles (two) to minimize
264 acquisition time. For this case, it has been shown that the flip angle choice resulting in the
265 best precision for VFA T1 estimates for a sample with a single T1 value (i.e. single tissue) are
266 the two flip angles that result in 71% of the maximum possible steady-state signal (i.e. at the
267 Ernst angle) (Deoni et al., 2003; Schabel & Morrell, 2008).

268 Time allowing, additional flip angles are often acquired at higher values and in between the two
269 above, because greater signal differences between tissue T1 values are present there (e.g. **Figure**
270 **2**). Also, for more than two flip angles, Equations 1 and 4 do not have the same noise weighting
271 for each fitting point, which may bias linear least-square T1 estimates at lower SNRs. Thus,
272 it has been recommended that low SNR data should be fitted with either Equation 1 using
273 non-linear least-squares (slower fitting) or with a weighted linear least-squares form of Equation
274 **4** (Chang et al., 2008).

275 Accurate knowledge of the flip angle values is very important to produce accurate T1 maps.
276 Because of how the RF field interacts with matter (Sled & Pike, 1998), the excitation RF field
277 (B1+, or B1 for short) of a loaded RF coil results in spatial variations in intensity/amplitude,
278 unless RF shimming is available to counteract this effect (not common at clinical field strengths).
279 For quantitative measurements like VFA which are sensitive to this parameter, the flip angle
280 can be corrected (voxelwise) relative to the nominal value by multiplying it with a scaling
281 factor (B1) from a B1 map that is acquired during the same session:

$$\theta_{corrected} = B_{_1}\theta_{nominal} \quad (6)$$

282 B1 in this context is normalized, meaning that it is unitless and has a value of 1 in voxels
283 where the RF field has the expected amplitude (i.e. where the nominal flip angle is the actual
284 flip angle). **Figure 6** displays fitted VFA T1 values from a Monte Carlo dataset simulated using
285 biased flip angle values, and fitted without/with B1 correction.

286 **Figure 6.** Mean and standard deviations of fitted VFA T1 values for a set of Monte Carlo
287 simulations (SNR = 100, N = 1000), simulated using a wide range of biased flip angles and
288 fitted without (blue) or with (red) B1 correction. Simulation parameters: TR = 25 ms, T1
289 = 900 ms, $\theta_{nominal} = 6^\circ$ and 32° (optimized values for this TR/T1 combination). Notice
290 how even after B1 correction, fitted T1 values at B1 values far from the nominal case (B1
291 = 1) exhibit larger variance, as the actual flip angles of the simulated signal deviate from the
292 optimal values for this TR/T1 (Deoni et al. 2003).

293 **Figure 7** displays an example VFA dataset and a B1 map in a healthy brain, along with the T1
294 map estimated using a linear fit (Equations 4 and 5).

295 **Figure 7.** Example variable flip angle dataset and B1 map of a healthy adult brain (left).
296 The relevant VFA protocol parameters used were: $TR = 15$ ms, $\theta_{nominal} = 3^\circ$ and 20° .
297 The T1 map (right) was fitted using a linear regression (Equations 4 and 5).

298 Benefits and Pitfalls

299 It has been well reported in recent years that the accuracy of VFA T1 estimates is very sensitive
300 to pulse sequence implementations (Baudrexel et al., 2017; Lutti & Weiskopf, 2013; Stikov
301 et al., 2015), and as such is less robust than the gold standard inversion recovery technique.
302 In particular, the signal bias resulting from insufficient spoiling can result in inaccurate T1
303 estimates of up to 30% relative to inversion recovery estimated values (Stikov et al., 2015).
304 VFA T1 map accuracy and precision is also strongly dependent on the quality of the measured
305 B1 map (Lee et al., 2017), which can vary substantially between implementations (Boudreau
306 et al., 2017). Modern rapid B1 mapping pulse sequences are not as widely available as VFA,
307 resulting in some groups attempting alternative ways of removing the bias from the T1 maps
308 like generating an artificial B1 map through the use of image processing techniques (Lieberman
309 et al., 2013) or omitting B1 correction altogether (Yuan et al., 2012). The latter is not
310 recommended, because most MRI scanners have default pulse sequences that, with careful
311 protocol settings, can provide B1 maps of sufficient quality very rapidly (Boudreau et al., 2017;
312 Samson et al., 2006; Wang et al., 2005).

313 Despite some drawbacks, VFA is still one of the most widely used T1 mapping methods in
314 research. Its rapid acquisition time, rapid image processing time, and widespread availability
315 makes it a great candidate for use in other quantitative imaging acquisition protocols like
316 quantitative magnetization transfer imaging (Cercignani et al., 2005; Yarnykh, 2002) and
317 dynamic contrast enhanced imaging (Li et al., 2018; Sung et al., 2013).

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